

Econometrics

Lab Hour – Session 3

Agustín Bénétrix
benetria@tcd.ie

Office hour:
Wednesday 4-5
Room 3021

Martin Schmitz
schmitzm@tcd.ie

Office hour:
Monday 5-6
Room 3021

Outline

- Importing the dataset
- Regression analysis in Microfit
 - Today: Heteroscedasticity
- Project time

Import Dataset

- Import to Microfit (using Sleep75.fit)
- Or using Sleep75.csv
 - Make sure you know how to import .csv files

Tasks

- Estimate the model

$$sleep = \beta_0 + \beta_1 totwrk + \beta_2 educ + \beta_3 age + \beta_4 age^2 + \beta_5 yngkid + \beta_6 male + u,$$

Output

Dependent variable is SLEEP
706 observations used for estimation from 1 to 706

| Regressor | Coefficient | Standard Error | T-Ratio[Prob] |
|-----------|-------------|----------------|-----------------|
| CONSTANT | 3840.9 | 239.4139 | 16.0427[.000] |
| TOTWRK | -.16342 | .018163 | -8.9974[.000] |
| EDUC | -11.7133 | 5.8720 | -1.9948[.046] |
| AGE | -8.6974 | 11.3291 | -.76771[.443] |
| AGESQ | .12844 | .13467 | .95375[.341] |
| YNGKID | -.022801 | 50.2764 | -.4535E-3[1.00] |
| MALE | 87.7546 | 34.6679 | 2.5313[.012] |

| R-Squared | .12275 | R-Bar-Squared | .11522 |
|----------------------------|----------|----------------------------|--------------------------|
| S.E. of Regression | 418.0269 | F-stat. | F(6, 699) 16.3018[.000] |
| Mean of Dependent Variable | 3266.4 | S.D. of Dependent Variable | 444.4134 |
| Residual Sum of Squares | 1.22E+08 | Equation Log-likelihood | -5259.3 |
| Akaike Info. Criterion | -5266.3 | Schwarz Bayesian Criterion | -5282.3 |
| DW-statistic | 1.9385 | | |

| Diagnostic Tests | | | |
|-------------------------------------------------------------------------|----------------|---|-------------|
| * Test Statistics * | LM Version | * | F Version * |
| * | * | * | * |
| * A:Serial Correlation*CHSQ(1)= .66603[.414]*F(1, 698)= .65911[.417]* | | | |
| * * | * | * | * |
| * B:Functional Form *CHSQ(1)= 1.4660[.226]*F(1, 698)= 1.4524[.229]* | | | |
| * * | * | * | * |
| * C:Normality *CHSQ(2)= 184.0682[.000]* | Not applicable | | * |
| * * | * | * | * |
| * D:Heteroscedasticity*CHSQ(1)= .82601[.363]*F(1, 704)= .82463[.364]* | | | |

A:Lagrange multiplier test of residual serial correlation
B:Ramsey's RESET test using the square of the fitted values
C:Based on a test of skewness and kurtosis of residuals
D:Based on the regression of squared residuals on squared fitted values

Note on Heteroscedasticity test

- White LM Test included in Microfit
- H_0 : Homoscedasticity
 - p-value above 10%
 - Thus, we can't reject the H_0

Tasks

- Calculate heteroscedasticity robust standard errors. Are these s.e. different from the usual ones?

Solution

Ordinary Least Squares Estimation

Based on White's Heteroscedasticity adjusted S.E.'s

Dependent variable is SLEEP

706 observations used for estimation from 1 to 706

| Regressor | Coefficient | Standard Error | T-Ratio[Prob] |
|-----------|-------------|----------------|-----------------|
| CONSTANT | 3840.9 | 259.1258 | 14.8223[.000] |
| TOTWRK | -.16342 | .020683 | -7.9014[.000] |
| EDUC | -11.7133 | 5.7475 | -2.0380[.042] |
| AGE | -8.6974 | 11.7869 | -.73789[.461] |
| AGESQ | .12844 | .13602 | .94426[.345] |
| YNGKID | -.022801 | 53.9053 | -.4230E-3[1.00] |
| MALE | 87.7546 | 35.5425 | 2.4690[.014] |

Task

- Find a model that allows the variance of u to differ between men and women (and not on any other factors)!

Solution

The assumption that the variance of u given all explanatory variables depends only on gender is

$$\text{Var}(u | \text{totwrk}, \text{educ}, \text{age}, \text{yngkid}, \text{male}) = \text{Var}(u | \text{male}) = \delta_0 + \delta_1 \text{male}$$

Then the variance for women is simply δ_0 and that for men is $\delta_0 + \delta_1$; the difference in variances is δ_1 .

Task

- Estimate the model for heteroskedasticity!
 - Take residuals from OLS equation.
 - Square the residuals
 - $\text{Residsq} = \text{RESIDUALS}^2$
- Is the variance higher for men or women?

Solution

After estimating the above equation by OLS, we regress \hat{u}_i^2 on $male_i$, $i = 1, 2, \dots, 706$ (including, of course, an intercept).

We can write the results as

$$\begin{aligned}\hat{u}^2 &= 189,359.2 & - & 28,849.6 \text{ } male & + \text{residual} \\ &(20,546.4) && (27,296.5)\end{aligned}$$

$$n = 706, R^2 = .0016.$$

Because the coefficient on $male$ is negative, the estimated variance is higher for women.

Output

Ordinary Least Squares Estimation

Dependent variable is RESIDSQ

706 observations used for estimation from 1 to 706

| Regressor | Coefficient | Standard Error | T-Ratio[Prob] |
|----------------------------|-------------|----------------------------|---------------|
| CONSTANT | 189359.2 | 20546.4 | 9.2162[.000] |
| MALE | -28849.6 | 27296.5 | -1.0569[.291] |
| ***** | ***** | ***** | ***** |
| R-Squared | .0015842 | R-Bar-Squared | .1660E-3 |
| S.E. of Regression | 359414.4 | F-stat. F(1, 704) | 1.1170[.291] |
| Mean of Dependent Variable | 173013.8 | S.D. of Dependent Variable | 359444.3 |
| Residual Sum of Squares | 9.09E+13 | Equation Log-likelihood | -10032.1 |
| Akaike Info. Criterion | -10034.1 | Schwarz Bayesian Criterion | -10038.6 |
| DW-statistic | 2.0385 | ***** | ***** |
| ***** | ***** | ***** | ***** |

Task

- Is the variance of u statistically different for men and women?

Solution

- No. The t statistic on *male* is only about -1.06 , which is not significant at even the 20% level against a two-sided alternative.

- Project time....